

# Superimposed grating wavelength division multiplexing in Ge-doped SiO<sub>2</sub>/Si planar waveguides

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**Abstract.** An improved model of wavelength division multiplexing (WDM) by superimposed gratings in planar waveguides has been developed. Based on this theory, principal design rules of  $N$ -channel WDM are established and a fanout capacity of 100 is estimated. Finally, four-channel WDM at 840 nm has been demonstrated on a Ge:SiO<sub>2</sub>/SiO<sub>2</sub>/Si planar waveguide, which was hydrogenated to enhance its photosensitivity. The superimposed gratings were written using a narrow linewidth KrF excimer laser in an interferometric setup used in inscribing fiber Bragg gratings. © 1998 Society of Photo-Optical Instrumentation Engineers. [S0091-3286(98)04402-X]

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## 1 Introduction

In today's world, where information technology is of great importance, transmission speeds in fiber optics are an important concern. It is well known that integrated wavelength division multiplexers (WDMs) are key elements for enhancing the transmission capacity of fiber optic communication systems. In view of the requirement for WDMs, several such integrated devices have been already demonstrated, based on different concepts. The curved-diffraction-grating WDM,<sup>1</sup> the Mach-Zehnder WDM,<sup>2</sup> and the arrayed-waveguide WDM<sup>3</sup> are examples. Recently an alternative WDM device technology that is relatively simple, compact, potentially implementable, and integrable with other telecommunication elements has been reported in Refs. 4 to 6. In that work a theoretical investigation has been reported on wavelength division using superposition of multiple Bragg gratings on a planar waveguide (Fig. 1). In this paper we first present an improved theoretical model, and on that basis we demonstrate a four-channel WDM accomplished by superimposing four Bragg gratings on a photosensitive planar waveguide.

## 2 Modeling

To study the effect of coupling between the superimposed gratings and to design the WDM properly, a theoretical model was developed from the coupled mode theory.<sup>4-6</sup> In

this model, the  $N$  gratings are designed so that each of them diffracts one particular wavelength  $\lambda_i$  to one particular direction  $\theta_{Si}$  for a common input angle  $\theta_R$ . The combined response of all the gratings to an input beam excitation at wavelength  $\lambda_R$  and incident angle  $\theta_R$  is calculated by solving a set of  $N + 1$  coupled-mode differential equations in the grating zone:

$$\cos \theta_R \frac{dR(z)}{dz} = -j \sum_{i=1}^N \kappa_i \exp(-j\Delta_i z) S_i(z), \quad (1)$$

$$\cos \Theta_{Si} \frac{dS_i(z)}{dz} = -j \kappa_i \exp(+j\Delta_i z) R(z)$$

$$\text{for } i = 1, \dots, N,$$

where  $R(z)$  is the amplitude of the input beam,  $S_i(z)$  and  $\Theta_{Si}$  are the amplitude and output angle of the diffracted beams,  $\kappa_i$  are the grating coupling coefficients as defined in Ref. 4, and  $\Delta_i$  are the phase-mismatch factors. The diffraction efficiency of each grating is then calculated using

$$\eta_i(z) = \frac{\cos \Theta_{Si}}{\cos \theta_R} |S_i(z)|^2. \quad (2)$$

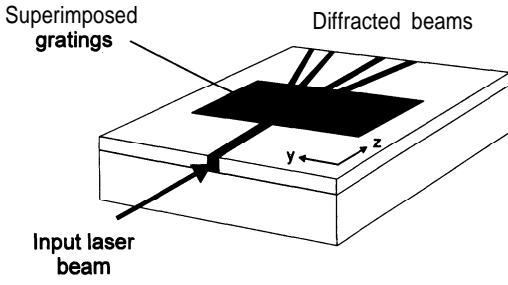


Fig. 1 A schematic diagram of a four-grating WDM on a planar waveguide.

### 3 Device Design

With the improved model, it was possible to quantify different regimes of integrating couplings, which help in the design of a device. In the case of strong coupling, superimposed gratings show very large deviations from the responses expected of individual sets of gratings. In this regime it is difficult, if not impossible, to construct a conventional WDM. On the other hand, in the **quasidecoupled** regime, where the wavelength and angular separation are larger, the superimposed gratings give nearly independent responses and the design of an N-channel WDM is relatively straightforward.

The criterion of quasidecoupling is simply given by

$$\Delta\lambda \geq 1.5 \Delta\lambda_{i0}, \quad (5)$$

where  $\Delta\lambda$  is the wavelength separation between the adjacent channels, and  $\Delta\lambda_{i0}$  is the total width at the first two zeros of the isolated grating spectrum (calculated as if the other gratings were absent). In the quasidecoupled regime, the analysis for an N-channel WDM is relatively straightforward. The expression for  $\Delta\lambda_{i0}$  as a function of the key structure and operation parameter assuming a perfect collimated input beam is given by<sup>7</sup>

$$\Delta\lambda_{i0} = \sqrt{3} \frac{\lambda_i^2 \cos \theta_{Si}}{n_e L_{ci} (1 - \cos(\theta_{Si} - \theta_R))} \quad (6)$$

where  $n_e$  is the guided-mode effective index.

This equation shows that the grating selectivity depends on both the grating length and the diffraction angle. The longer the grating and the larger the diffraction angle, the more selective is the grating ( $\Delta\lambda_{i0}$  diminishes). Therefore, the design of a WDM with evenly spaced channels with a spacing of  $\Delta\lambda_{\text{WDM}}$  around a central wavelength  $\lambda_c$  is constrained by a minimal diffraction angle under which the gratings will be strongly coupled and will give a distorted spectrum. For  $\theta_R = 0$ , which is the most convenient configuration, one calculates

$$\theta_{\min} = \cos^{-1} \left[ \left( 1 + \frac{1.5\sqrt{3}}{n_e L_{ci}} \frac{\lambda_c^2}{\Delta\lambda_{\text{WDM}}} \right)^{-1} \right]. \quad (7)$$

Thus,  $\theta_{\min}$  will depend on the coupling length. The longer the  $L_{ci}$ , the smaller the minimal diffraction angle. This analysis only shows the range of “good” diffraction angles,  $|\theta_{Si}| \geq \theta_{\min}$ , but individual adjustments of either the grating’s length or its strength and good input conditions are required to ensure high diffraction efficiencies.\*

In Ref. 6 the angular spacing between channels was examined by looking at the inter-grating coupling that can occur for close diffraction angles. It was found that the minimal angle spacing between channels, above which the coupling can be neglected, is of the order of a few milliradians. All considered, in the quasidecoupled regime, we find that the maximum **fanout** capacity of the superimposed grating WDM is of the order of 100, thus being limited only by the maximal index change inducible in the material.

The coupling coefficient describes the strength with which a grating interacts with a guided wave. The **phase-mismatch factor** is a measure of the deviation from the Bragg condition and defines the maximal energy exchange between the wave  $R$  and  $S_i$ . When the Bragg condition is satisfied,  $\Delta_i = 0$ , and there is a maximal transfer of energy at the coupling length  $L_{ci}$  ( $\eta_i = 1$  if there is only one grating). For  $\Delta_i \gg 1$  there is no transfer of energy ( $\eta_i \ll 1$ ). The phase-mismatch factor is a key parameter that determines the wavelength and angular selectivity of the gratings and thus their coupling when they are superimposed.

Following the work published in Ref. 6, an improved calculation of the phase-mismatch factor is accomplished by including the angular dispersion  $\Delta\theta_{Si}$  that results from a wavelength dispersion  $\Delta\lambda$  of the input beam. As shown in Fig. 2, the diffraction angle of an input wavelength  $\lambda_R = \lambda_i + \Delta\lambda$  is found to be

$$\theta_{Si} = \theta_{Si} + \Delta\theta_{Si} \approx \theta_{Si} + \frac{\sin \theta_{Si} - \sin \theta_R}{\cos \theta_{Si}} \frac{\Delta\lambda}{\lambda_i}, \quad (3)$$

where the phase-mismatch factor is simply given by

$$\Delta_i = \beta_R \cos(\theta_{Si} + \Delta\theta_{Si}) - (\beta_R \cos \theta_R + K_i \cos \phi_i). \quad (4)$$

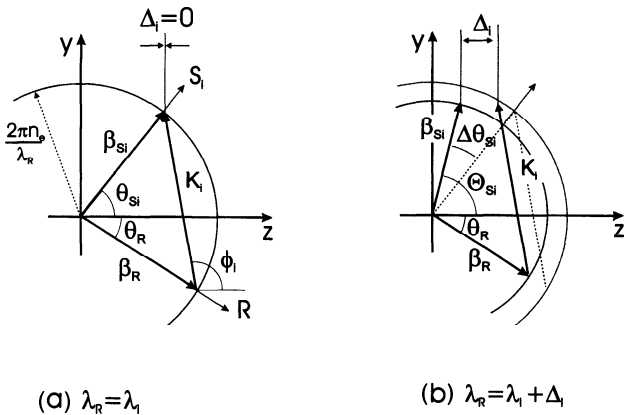


Fig. 2 A  $\beta$  diagram of the interaction of the input beam at wavelength  $\lambda_R$  and the grating (a) at the **Bragg** condition and (b) off the Bragg condition.

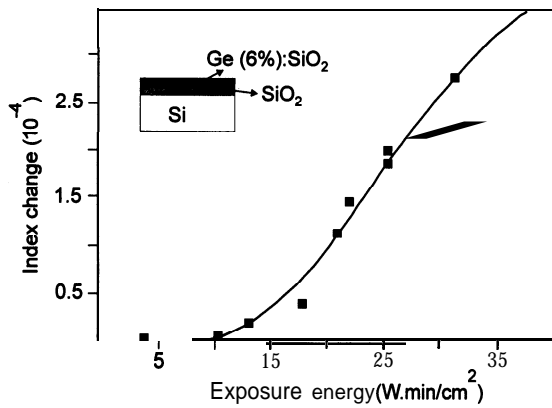


Fig. 3 Photosensitivity characterization of the Ge-doped-silica-on-silicon planar waveguide.

## 4 Experiments

The guiding structure of the photosensitive Ge-doped silica-on-silicon planar waveguides that was used in these experiments is shown in the inset of Fig. 3. These guides were first placed in a high-pressure hydrogen chamber that was maintained at 1500 psi at room temperature for several days, to increase their photosensitivity at the 245-nm UV band. Following the hydrogenation treatment, a two-laser beam interferometric setup was used to inscribe the gratings on the waveguides. The laser beams used in the interferometer were obtained from a narrow-linewidth KrF excimer laser.<sup>9</sup> Prior to writing the multiple gratings, the waveguide material was characterized in term of index change versus UV exposure in an attempt to optimize the grating diffraction efficiency. This was achieved by inscribing a simple 5-mm-long Bragg gratings on identical waveguides over different exposure times. From the reflection efficiencies of the well-defined Bragg gratings inscribed on the different waveguides it was possible to estimate the index of refraction change for the different exposure times (see Fig. 3). Following this, four 5-mm-long superimposed gratings were successively exposed for 15 min with beam energy of 100 mJ/pulse at 30 Hz. They were designed to diffract at  $\lambda_i = 830, 840, 850,$  and  $860$  nm at  $\theta_{Si} = +32, -26, -30,$  and  $+28$  deg, respectively ( $\theta_R$

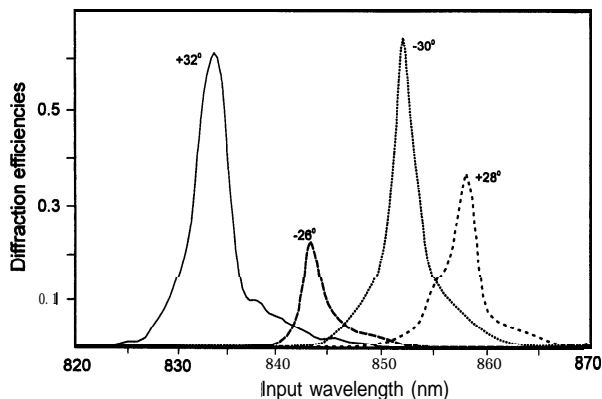


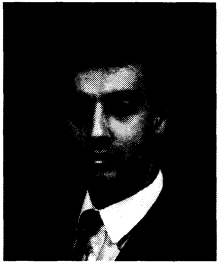
Fig. 4 Diffraction spectral response of the four-channel WDM.

$=0$ ). The choice of the diffracted wavelengths is dictated by the range of tunability of the laser used for the characterization.

To measure the diffraction efficiency versus input wavelength at each  $\theta_{Si}$ , a beam of a Ti:sapphire tunable laser was coupled into the  $TE_0$  guided mode with a prism, and the measurements of the WDM characteristics were taken from the output edge of the waveguide. The diffraction efficiencies vary from 62% to 21%, while the FWHMs were around 3 nm. This is approximately 6 times broader than the theoretical values given by Eq. (6), whereas the cross talks are between  $-10$  and  $-15$  dB (Fig. 4). The broader than expected FWHMs prompted us to perform a secondary experiment to inspect the uniformity of the index modulation profiles. By illuminating the sample with a coherent visible beam from the top (nonguided light) we generated scattered beams corresponding to the different orders of the Raman-Nath diffraction through the thin layer of the grating. Because the intensity of each of them is proportional to the local index modulation, the use of a large-diameter incident beam allows the observation of the index modulation profile over the whole grating area. As suspected, highly nonuniform gratings were been observed in all fabricated samples. We attribute this to the nonuniformity of the excimer laser writing beam itself, which was working at barely above the threshold due to the intracavity etalons used in narrowing the linewidth of the laser. This nonuniformity of the index modulation over the grating area explains the broadening of the spectral response and the relatively high level of cross talk. It also partially explains the relatively low diffraction efficiencies, which should be improved with better control of the grating strength (i.e., of the exposure). However, as a proof-of-feasibility demonstration, the four-channel WDM implemented in silicon glass exhibited satisfactory functionality of wavelength demultiplexing.

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Biographies and photographs of other authors not available.